

Measurement of The Polarization in $D^0 \rightarrow VV$ Decays On BES-III

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The 10th National Conference of Particle Physics

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Physics Motivations

- Precise measurement of longitudinal polarization can enhance our understanding of $D^0 \rightarrow VV$ decays.
- It will be interesting to compare the results of D^0 and \bar{D}^0 decay to a common final state.
- Provide a new method to measure the mixing and CP violating parameters[†].

Possible decay channels on BES-III

- $D^0 \rightarrow \bar{K}^{*0} \rho^0$ $(1.5 \pm 0.33)\%$
- $D^0 \rightarrow \bar{K}^{*0} \omega$ $(1.1 \pm 0.04)\%$
- $D^0 \rightarrow K^{*0} \bar{K}^{*0}$ $\sim 0.27\%$

[†]For more information, please refer to I. Dunietz *et al.*, Phys.Rev.D 43, 1991

Decay Amplitudes in Helicity Formalism

The $D^0 \rightarrow VV$ decays can be described by three amplitudes, which can be expressed in three different bases:

- In the *partial wave basis*, the amplitudes are related to relative angular momentum L , corresponding to the S , P and D waves.
- In the *helicity basis*, the amplitudes correspond to *helicity eigenstates*, including *longitudinal* ($\lambda = 0$) part and *transverse* ($\lambda = \pm 1$) part.

$$\text{longitudinal } (\lambda = 0): A_0 = -\frac{1}{\sqrt{3}}S + \sqrt{\frac{2}{3}}D$$

$$\text{transverse } (\lambda = +1): A_{+1} = \frac{1}{\sqrt{3}}S + \frac{1}{\sqrt{6}}D + \frac{1}{\sqrt{2}}P$$

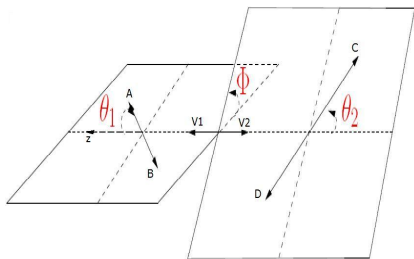
$$\text{transverse } (\lambda = -1): A_{-1} = \frac{1}{\sqrt{3}}S + \frac{1}{\sqrt{6}}D - \frac{1}{\sqrt{2}}P$$

- To form *CP eigenstates*, the above decay amplitudes can be rewrote in their linear combinations, this is called the *transversity formalism*.

Angular Distribution in Helicity Formalism

Definition (Helicity angle)

- Choose z axis to be along the line of flight of V_1 .
- The helicity angle θ_1 in the decay of V_1 is defined as the angle between z and direction of A in rest frame of V_1 .
- The helicity angle θ_2 is defined likewise.



General angular distribution:

$$\begin{aligned} \frac{1}{\Gamma} \frac{d^3\Gamma}{d \cos \theta_1 d \cos \theta_2 d\phi} &= \frac{9}{16\pi} \frac{1}{|A_0|^2 + |A_{+1}|^2 + |A_{-1}|^2} \left\{ \frac{1}{2} \sin^2 \theta_1 \sin^2 \theta_2 (|A_{+1}|^2 + |A_{-1}|^2) \right. \\ &+ 2 \cos^2 \theta_1 \cos^2 \theta_2 |A_0|^2 + \sin^2 \theta_1 \sin^2 \theta_2 [\cos 2\phi \mathcal{R}e(A_{+1} A_{-1}^*) \\ &- \sin 2\phi \mathcal{I}m(A_{+1} A_{-1}^*)] - \frac{1}{2} \sin 2\theta_1 \sin 2\theta_2 [\cos \phi \mathcal{R}e(A_{+1} A_0^* + A_{-1} A_0^*) \\ &\left. - \sin \phi \mathcal{I}m(A_{+1} A_0^* - A_{-1} A_0^*) \right\} \end{aligned}$$

Signal sample:

- Decay mode: $\psi(3770) \rightarrow D^0 \bar{D}^0$, $D^0 \rightarrow (K_S \pi^0)_{\bar{K}^{*0}} (\pi^+ \pi^-)_{\rho^0}$
- $\mathcal{BR}(\psi(3770) \rightarrow D^0 \bar{D}^0) \sim 57.2\%$, $\mathcal{BR}(D^0 \rightarrow K_S \pi^0 \pi^+ \pi^-) \sim 0.50\%$
- In this analysis, 90K signal events are generated and about 50K events are finally used to create the signal sample.

Background sample:

- 3.5M $\psi(3770)$ inclusive decay events are used to build background sample.
- In both signal and background data, the input value of longitudinal polarization fraction (f_L) is 0.33.
- Background and signal samples are generated under BOSS6.3.1.

Event Selection

- Good photon cuts:

$$E_\gamma \geq 20 \text{ MeV}; \quad \theta \geq 20^\circ; \quad \phi \geq 20^\circ$$

- Use kinematic fit for K_S and π^0 reconstruction:

$$\chi^2(K_S \rightarrow \pi^+\pi^-) \leq 500; \quad \chi^2(\pi^0 \rightarrow \gamma\gamma) \leq 500$$

- Use ParticleID to separate K/π

- Use kinematic fit to reconstruct D^0 :

The $(K_S\pi^0\pi^+\pi^-)$ combination with least $\chi^2(\leq 50)$ is selected.

- Mass window cuts:

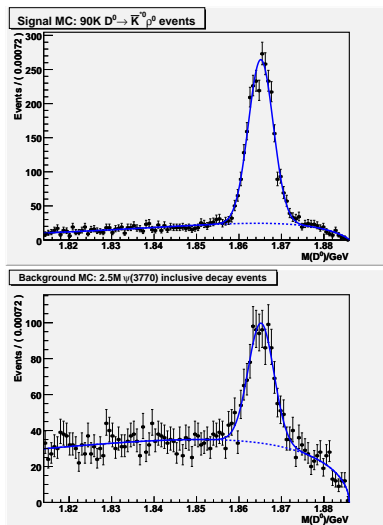
$$\Delta M_D = |M_{D^0} - 1.851| \leq 0.012;$$

$$\Delta M_K = |M_{\bar{K}^{*0}} - 0.892| \leq 0.12;$$

$$\Delta M_\rho = |M_{\rho^0} - 0.771| \leq 0.16;$$

$$\Delta M_K^2 + \Delta M_\rho^2 < 0.02;$$

D^0 Candidate Reconstruction



- Fitting results of signal sample:
 $M_{D^0} = 1.86514 \pm 0.00007$ GeV
 $\sigma = (2.93 \pm 0.07) \times 10^{-3}$ GeV
 $N_{Sig} = 2451 \pm 62$
 $N_{Bkg} = 1813 \pm 57$
 $\epsilon = 2.72\%$
- Fitting results of inclusive decay sample:
 $M_{D^0} = 1.8652 \pm 0.0002$ GeV
 $\sigma = (3.02 \pm 0.02) \times 10^{-3}$ GeV
 $N_{Sig} = 702 \pm 52$
 $N_{Bkg} = 3090 \pm 71$
- According to the input branch ratio, about 356 events are expected in the signal region. The rest 346 events are mainly the contribution of non-resonant background.

Preparation of Data Samples With Given f_L

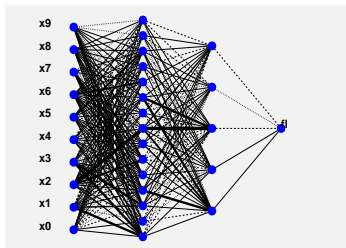
Data sample with different f_L and number of signal events N_S can be created in the following procedure:

- simplified 1-D angular distribution function:

$$\frac{d\Gamma}{d\cos\theta_1} = \frac{3}{4}[f_L \cdot 2\cos^2\theta_1 + (1 - f_L)\sin^2\theta_1]$$

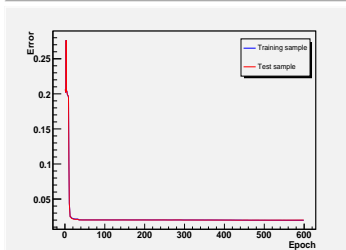
- Use distribution function at $f_L = 1$ and $f_L = 0$ to make longitudinal and transverse samples respectively.
- The signal events are subtracted from the inclusive decay sample.
- For particular f_L and N_S , randomly select and combine corresponding number of longitudinal, transverse and background events.
- With different seeds for random number, different samples with the same f_L and N_S can be generated.

Configuration and Training of ANN



ANN configuration:

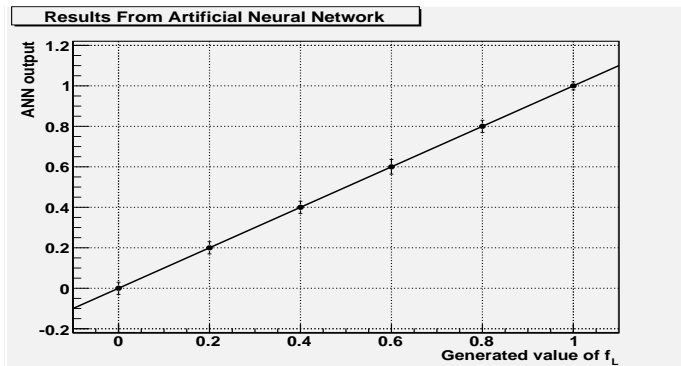
- The angular distribution is discretized into 10 bins as the input of ANN.
- Two hidden layers, with 20 and 5 neurons.
- The configuration parameters are preliminarily optimized.



ANN training:

- Training data:
Set $f_L = 0, 0.01, 0.02, \dots, 1.00$, six different data sample are generated and discretized at each f_L value.
- ANN is trained for 600 training cycles

Result and Error Estimation



- The error bar is defined as the standard deviation of ANN output for 100 different data samples at each fixed f_L .
- The data sample used as the ANN input contains approximately 850 signal events.

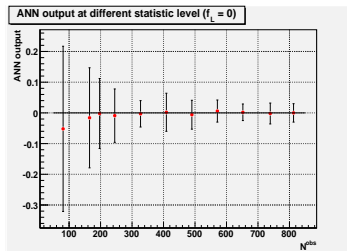
Potential of BES-III on Measuring f_L

- The observable number of events N^{obs} is related to $N(D^0\bar{D}^0)$ by the following formula:

$$N^{obs} = N(D^0\bar{D}^0) \times \epsilon_{tag} \times \mathcal{BR}(D^0 \rightarrow (K_S\pi^0)_{\bar{K}^*0}(\pi^+\pi^-)_{\rho^0}) \times \epsilon_{Rec}$$

- Taking $\epsilon_{tag} \sim 10\%$, $\mathcal{BR}(D^0 \rightarrow \bar{K}^*0\rho^0) = 0.50\%$, $\epsilon_{Rec} \sim 2.72\%$, we have:

$$N^{obs} = N(D^0\bar{D}^0) \times 1.36 \times 10^{-5}$$



- With one year of data taking at \mathcal{L}_{peak} , we can get about 18×10^6 $D^0\bar{D}^0$ pairs, the according statistical error is ± 0.1 .
- In four years of running, about 72×10^6 $D^0\bar{D}^0$ pairs will be collected, therefore the statistical error of f_L would be ± 0.03 .

Binned Maximum Likelihood Fit

- ML fit to extract signal yields and f_L in case of small signal yields and/or large background
- Likelihood function:

$$\mathcal{L} = \frac{e^{-(N_S+N_B)}}{N_{evt}!} \prod_{i=1}^{N_{evt}} (N_S \mathcal{P}_S + N_B \mathcal{P}_B)$$

\mathcal{P}_S : PDF of signal, generated by theoretical PDF multiplied with detector acceptance

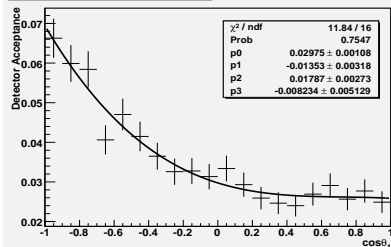
\mathcal{P}_B : PDF of background, generated by fitting background with a 3-order polynomial

- Fitting variable: currently only $\cos \theta_1$. Other variables including $\cos \theta_2$, ϕ , m_{D_0} , decay time, etc. can also be added in the future analysis.
- Performance of fitter is checked with toy MC data.

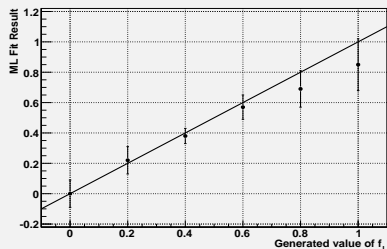
Result from ML Fit

- The reconstruction efficiency and background are both fitted with a 3-order polynomial.
- The data sample used in ML fit contains approximately 850 signal events.
- A systematic bias is found at high f_L value.

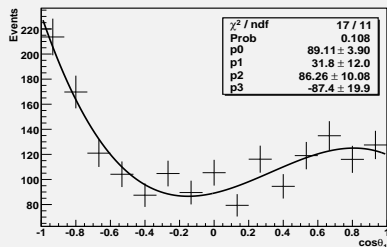
Detector Acceptance vs. $\cos\theta_1$



Results From Binned ML Fit



Background parameterization



- By using either ANN or maximum likelihood fitting, we are able to achieve much better accuracy of polarization measurement (compared with PDG current value) after one year of data taking.
- ANN method requires much less effort concerning reconstruction efficiency and background parametrization, yet gives results with higher accuracy.
- The primary bottleneck of this analysis is the low reconstruction efficiency caused by π^0 in the final states. By switching to charged final states, the result could be greatly improved.

Thank you!

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