

Physics at TeV Energy Scale

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I. Why TeV Scale Is Specially Important?

- SM is $SU(3)_c \times SU(2) \times U(1)$ gauge theory.

$$M_g, M_\gamma = 0,$$

$$M_W = 80.403 \pm 0.029 \text{ GeV}, \quad M_Z = 91.1876 \pm 0.0021 \text{ GeV}.$$

- Renormalizability of the EW gauge theory requires the Lagrangian to be exactly $SU(2) \times U(1)$ symmetric, while all mass terms

$$- M_W^2 W_\mu^i W^{i\mu}, \quad - m_f (\bar{\psi}_L \psi_R + \bar{\psi}_R \psi_L)$$

break the $SU(2) \times U(1)$ symmetry, so that they cannot occur in the Lagrangian.

In the Lagrangian (equations of motion), all particles are massless.

Where do the observed nonvanishing particle masses come from?

- In quantum field theory,

$$F_{obs} = \langle \textit{phys. state} | F_{op} | \textit{phys. state} \rangle$$

↑

asymm.

↑

symm.

↑

asymm.

$$| \textit{phys. state} \rangle = a^\dagger \dots \dots b^\dagger \dots \dots | 0 \rangle$$

↑

asymm.

↑

symm.

↑

asymm.

Observed particle masses can be nonzero if the physical ground state is asymmetric.

symmetric Lagrangian \implies asymmetric vacuum
spontaneous symmetry breaking (SSB).

- SM introduces elementary Higgs field ϕ and Higgs potential

$$V(\phi) = -\mu^2|\phi|^2 + \lambda|\phi|^4, \quad \lambda > 0$$

to obtain $\langle\phi\rangle^2 = v^2 \equiv \frac{\mu^2}{\lambda} \neq 0$.

$$v = 246 \text{ GeV}$$

can give the measured values of M_W and M_Z .

Higgs boson H ($\phi = v + H$) is the signal. So far H is not found.

LEP direct search bound:

$$m_H > 114.4 \text{ GeV}.$$

With $m_t = 170.9 \text{ GeV}$, LEP precision data



$$m_H \not> 182 \text{ GeV}, \quad 95\% \text{ CL}.$$

- In SM, Yukawa coupling $y_f \bar{\psi} \phi \psi \implies m_f = y_f \frac{v}{\sqrt{2}}$ is put in by hand.
Fermion masses are free parameters in SM.
- The origin of particle masses:

Newton:

$$m_0 \frac{d^2 \vec{x}}{d t^2} = \vec{f}$$

Einstein:

$$E = mc^2 = \frac{m_0 c^2}{\sqrt{1 - \frac{v^2}{c^2}}} \approx m_0 c^2 + \frac{1}{2} m_0 v^2 + \dots$$

Static energy:

$$E_0 = m_0 c^2$$

$$m_0 = ?$$

$v = 246 \text{ GeV}$

$$v = 246 \text{ GeV}$$

$$m_0 c^2 = E_0 \propto v$$

- SM Higgs sector is not a self-consistent theory.

★ Triviality:

Suppose SM is valid when $E \leq E_{max}$. Summing up all leading logarithm corrections: $\lambda \xrightarrow{E_{max} \rightarrow \infty} 0$. inconsistent !

There must be a scale of new physics Λ so that $E_{max} \not\gg \Lambda$.

★ Unnaturalness: $m_H^2 = m_{H0}^2 + \delta m_H^2$

$$\text{SM: } \implies \delta m_H^2 = A\Lambda^2, \quad m_{H0}^2 = B\Lambda^2 \quad [A, B = O(1)]$$

$$m_H^2 = (A + B)\Lambda^2$$

Possible new physics scale is $\Lambda \sim M_P \sim 1.22 \times 10^{19} \text{ GeV}$.

Then
$$A + B = \frac{m_H^2}{M_P^2} \sim 10^{-34},$$

requiring A, B to be of the precision of 34 digits. Unnatural !.

Naturalness requires $\Lambda \sim \text{TeV}$.

- If there are only presently discovered particles, the cross section of $WW \rightarrow WW$ will increase with the c.m. energy E . When $E \geq 1.2 \text{ TeV}$, the cross section will be so large that it violates the conservation of probability (unitarity of S-matrix). So there must be yet undiscovered particle(s) below 1.2 TeV – **(unitarity bound)** !
- We see that, in EW theory, all masses come from the VEV $v \neq 0$ breaking $SU(2) \times U(1)$. EWSBM is not clear yet. Probing EWSBM concerns the understanding of the original of all particle masses.
- We also see that TeV scale is the scale of discovering new particle(s) or going beyond the SM.
- Building high energy colliders covering the TeV scale will be able to explore the mechanism of mass generation and/or find out new physics beyond the SM.

II. TeV Colliders

- **LHC:**

14 TeV pp collider, designed luminosity: $\int_{yr} \mathcal{L} dt = 10^{34} \text{ cm}^{-2}\text{s}^{-1}$.

Parameter	Phase A	Phase B	Phase C	Nominal
k / no. bunches	43-156	936	2808	2808
Bunch spacing (ns)	2021-566	75	25	25
N (10^{11} protons)	0.4-0.9	0.4-0.9	0.5	1.15
Crossing angle (μrad)	0	250	280	280
$\sqrt{(\beta^*/\beta_{nom}^*)}$	2	$\sqrt{2}$	1	1
σ^* (μm , IR1&5)	32	22	16	16
L ($\text{cm}^{-2}\text{s}^{-1}$)	$6 \times 10^{30} - 10^{32}$	$10^{32} - 10^{33}$	$(1-2) \times 10^{33}$	10^{34}
Year (?)	2008	2009	2009-2010	> 2010

- ★ Advantage: parton colliding energy up to a couple of TeV
- ★ Sortcoming: large hadronic bkgd

LHC: discovery machine

- **ILC:**

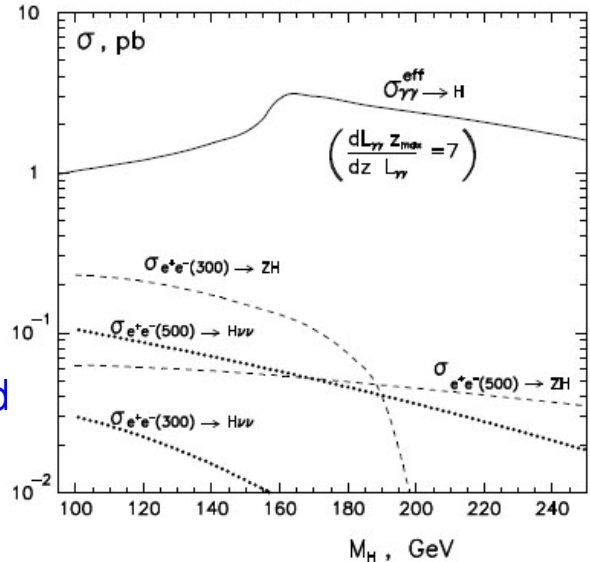
e^+e^- collider (in R&D)

Phase I: $200 \text{ GeV} \leq E \leq 500 \text{ GeV}$ (adjustable)

Phase II: $E \sim 1 \text{ TeV}$

Photon collider can be made by means of laser back-scattering.
Good for studying Higgs boson.

- ★ Advantage: small hadronic bkgd
- ★ Sortcoming: expensive for increasing energy



ILC: discovery and precision measurement machine

- More higher energy colliders are under consideration.

III. Examples of New Physics Models

- SUSY (MSSM)

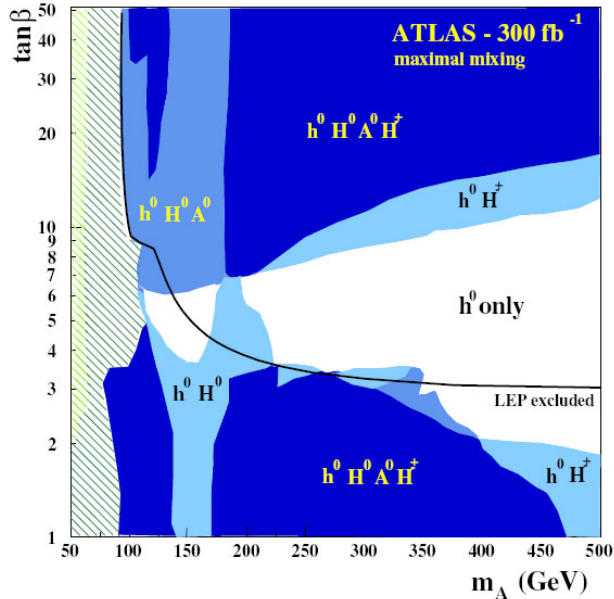
- ★ SUSY partners: $\tilde{W}^\pm \dots, \tilde{g}, \tilde{q}, \tilde{l}^\pm \dots$. Can solve the **triviality** and **fine-tuning** problems.

- ★ Can accommodate SUSY GUT $M_{GUT} \sim 5 \times 10^{16}$ GeV, and **radiative EWSB**.

- ★ Two Higgs doublets $\implies h^0, H^0, A^0, H^\pm$.

Two loop $\implies m_h \not\approx 135$ GeV.

- ★ LHC coverage:



- ★ sparticles not found \implies SUSY is broken, SUSY breaking mechanism not clear (general description: 105 free parameters).

$$\star \Delta m_H^2 \sim (M_{SUSY}^2 - M_{SM}^2) \frac{\lambda_f^2}{16\pi^2} \ln \left(\frac{\Lambda}{M_{SUSY}} \right).$$

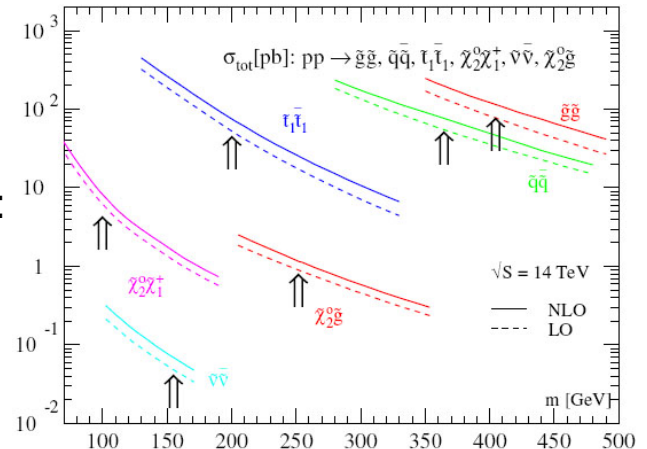
To avoid fine-tuning, $M_{SUSY} \not\approx \text{TeV}$ (low energy SUSY).

- ★ LHC, ILC: can find sparticles.

- ★ ILC: can make precision measurement of sparticle masses:

$$\begin{aligned} \delta m_{\tilde{t}, \tilde{b}} &= 1 \text{ GeV}, \\ \delta m_{\chi^{\pm, 0}} &= 0.1 - 1 \text{ GeV}, \\ \delta m_{\tilde{l}, \tilde{\nu}} &= 0.05 - 0.3 \text{ GeV}, \\ \delta m_{\tilde{\tau}, \tilde{\nu}_\tau} &= 0.6 \text{ GeV}. \end{aligned}$$

can test SUSY breaking mechanism.



- **Technicolor (TC)**

- ★ Abandon ϕ to avoid **triviality** and **fine-tuning**. Introduce new strong interactions **TC** and new fermions to develop

$$\langle \bar{\psi}\psi \rangle \neq 0 \implies v \neq 0.$$

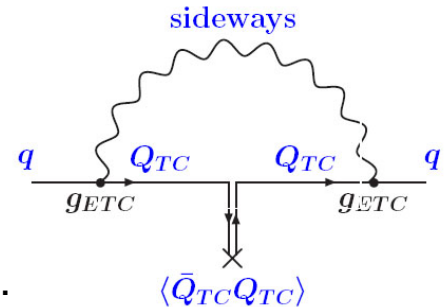
- ★ Yukawa interaction is dynamically induced

- ★ Original **QCD-like TC model** is **ruled out** by LEP precision data (**S** parameter **too large**).

- ★ Improved models associated with **Topcolor (TC2)** [Hill (1995); Lane, Eichten (1995), etc]. Consistent with LEP data [Chivukula, Terning (1996); Yue, Kuang, Wang, Li (2000)]

- ★ Signals: ρ_{TC} , π_{TC} , π_t , \dots .

- ★ Attempt to account for **CKM** matrix and **CP violation** [Martin, Lane (2005)].



● Top Quark Seesaw

[Dobrescu, Hill (1998); Chivukula, Dobrescu, Georgi, Hill (1999)]

★ Introduce topcolor group: $G_{tc} = SU(3)_1 \times SU(3)_2$ and new strong interaction group G breaking $G_{tc} \rightarrow SU(3)_{QCD}$.

★ introduce $SU(2)_W$ -singlet quark χ with proper $U(1)_Y$ quantum number. Topcolor causes the bound state scalar

$$\varphi = \begin{pmatrix} \overline{\chi_R} t_L \\ \overline{\chi_R} b_L \end{pmatrix}$$

φ behaves like a Higgs doublet. $\langle \varphi \rangle = v$ breaks EW symmetry.

★ Dynamics leads to

$$m_t \approx m_{t\chi} \frac{\mu_{\chi t}}{\mu_{\chi\chi}} \sim 174 \text{ GeV}$$

★ $m_H \sim 1 \text{ TeV}$ [He, Hill, Tait (2002)].

● Little Higgs

[Arkani-Hamed, Cohen, Georgi, Gregoire, Schmaltz, Wacker, Walker (2001–2005)]

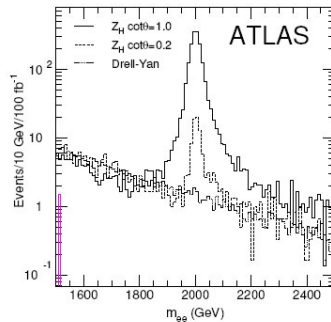
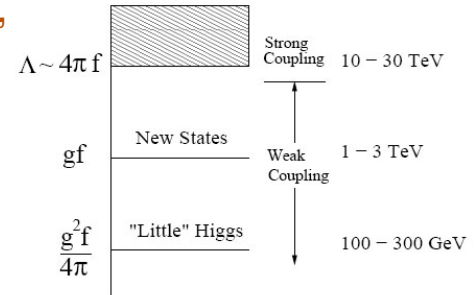
★ Strong interaction at $\Lambda \approx 10 \sim 30 \text{ TeV}$

pseudo Goldstone bosons (PGBs).

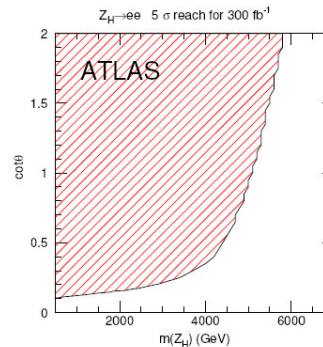
★ Heavy states at $gf \approx 1 \sim 3 \text{ TeV}$

★ Same spin particles cancel quadratic divergences to keep one or two PGBs light, ($100\text{--}300 \text{ GeV}$), as light Higgs boson(s) ϕ , $\langle \phi \rangle = v$ breaks $SU(2) \times U(1)$

★ Phenomenology of $SU(5)/SO(5)$ model [Han, Logan, McElrath, Wang (2003); Burdman, Perelstein, Pierce (2002)]



(a)

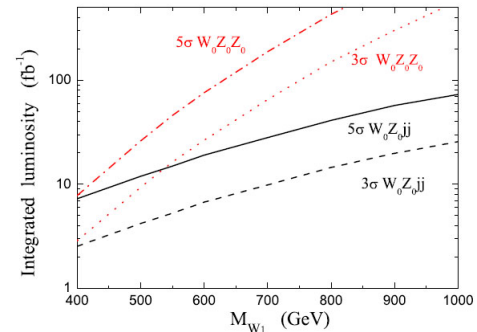
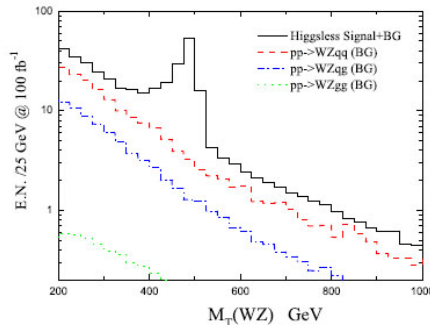
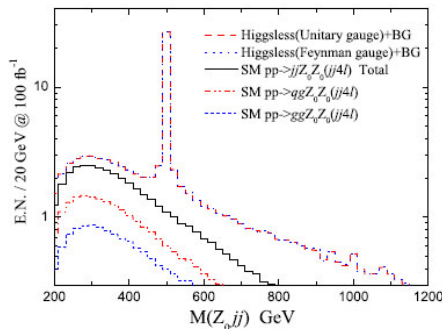


(b)

● Higgsless Model Based on Extra Dimension

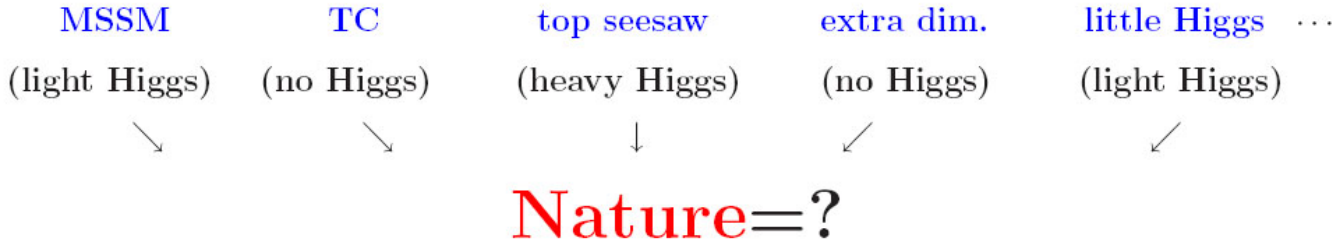
- ★ Higgsless model in 5-dim with broken $SU(2) \times U(1)$ built by imposing boundary conditions in the 5th-dim [Csaki *et al.* (2004)]
- ★ By means of **dimension deconstruction** Higgsless model can be constructed in 4-dim gauge theories with $SU(2) \times U(1)$ broken **spontaneously** by strong dynamics, and boundary condition in the 5th-dim can be **induced** by diagonalizing the mass matrix. Minimal model contains extra W_1 and Z_1 with $400 \text{ GeV} \leq M_{W_1} \leq 1 \text{ TeV}$. Can make $S, T, U \approx 0$ [He (2004); Chivukula *et al.* (2005)].
- ★ LHC signals: [Tsinghua-MSU (2007)]

$$pp \rightarrow W_1^* Z_0 \rightarrow W_0 W_0 Z_0, \quad pp \rightarrow W_1^* jj \rightarrow W_0 Z_0 jj$$



IV. Perspectives of LHC and ILC Expts

- General No-Lose Probe of New Physics Effects



No hint that nature can be described by one of the known models.

General no-lose probe is needed.



Effective couplings of known particles reflect the effect of new physics.

How to measure effective couplings at LHC and ILC?

- What If Only a Light Higgs Resonance Is Found?

Is it a SM Higgs or a Higgs in new physics?

Need to test Higgs couplings.

- ★ Testing gauge couplings of the Higgs boson

$$\begin{aligned} \mathcal{L}_{eff}^{HVV} = & g_{H\gamma\gamma} H A_{\mu\nu} A^{\mu\nu} + g_{HZ\gamma}^{(1)} A_{\mu\nu} Z^\mu \partial^\nu H + g_{HZ\gamma}^{(2)} H A_{\mu\nu} Z^{\mu\nu} \\ & + g_{HZZ}^{(1)} Z_{\mu\nu} Z^\mu \partial^\nu H + g_{HZZ}^{(2)} H Z_{\mu\nu} Z^{\mu\nu} \\ & + g_{HWW}^{(1)} (W_{\mu\nu}^+ W_-^\mu \partial^\nu H + h.c.) + g_{HWW}^{(2)} H W_{\mu\nu}^+ W_-^{\mu\nu} \end{aligned}$$

SM: $g_{HVV}^{(i)} = 0.$

- ★ LHC

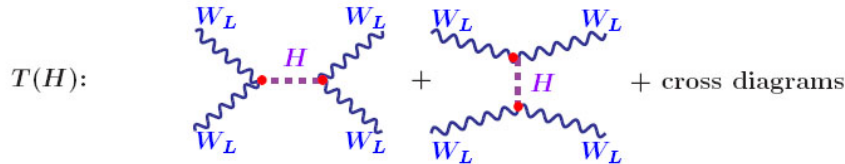
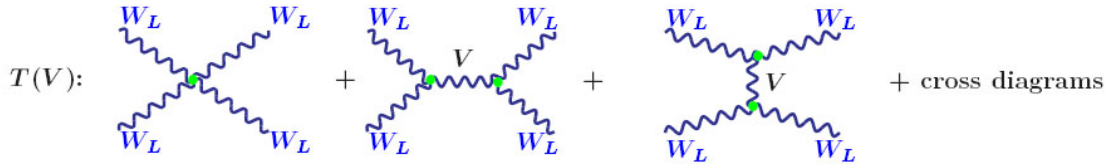
- [Plehn, Rainwater, Zeppenfeld (2003)] WW fusion at the LHC:

$$pp \rightarrow qq' H, H \rightarrow \gamma\gamma, \tau^+ \tau^-:$$

$$1\sigma \text{ (stat.): } |g_{HWW}^{(2)}| \geq 0.1 \text{ TeV}^{-1}.$$

- [Zhang, Kuang, He, Yuan (2003)]

$$W^+W^+ \rightarrow W^+W^+ \rightarrow l^+\nu_l l^+\nu_l$$



$$\begin{aligned}
 3\sigma \text{ (stat.)} : \quad & |g_{HWW}^{(1)}| \geq 0.075 \text{ TeV}^{-1}, & |g_{HWW}^{(2)}| \geq 0.15 \text{ TeV}^{-1}, \\
 & |g_{HZZ}^{(1)}| \geq 0.075 \text{ TeV}^{-1}, & |g_{HZZ}^{(2)}| \geq 0.058 \text{ TeV}^{-1}, \\
 & |g_{HZ\gamma}^{(1)}| \geq 0.041 \text{ TeV}^{-1}, & |g_{HZ\gamma}^{(2)}| \geq 0.032 \text{ TeV}^{-1}, \\
 & |g_{H\gamma\gamma}| \geq 0.035 \text{ TeV}^{-1}.
 \end{aligned}$$

★ ILC:

- [Hagiwara, Ishihara, Kamoshita, Kniehl (2000)] ILC:

$$e^+e^- \rightarrow HZ, \quad H \rightarrow b\bar{b}, \quad Z \rightarrow f\bar{f}:$$

$$2\sigma \text{ (stat.):} \quad |g_{HZZ}^{(i)}|, |g_{HZ\gamma}^{(i)}| \geq 10^{-3} - 10^{-2} \text{ TeV}^{-1}.$$

- [Han, Kuang, Zhang (2005)] $\gamma\gamma$ colliders:

$$\gamma\gamma \rightarrow ZZ \rightarrow 4 \text{ jets}$$

3σ (stat.) :

$$500 \text{ GeV ILC} \quad |g_{H\gamma\gamma}| \geq 0.023 \text{ TeV}^{-1},$$

$$1 \text{ TeV ILC} \quad |g_{H\gamma\gamma}| \geq 0.010 \text{ TeV}^{-1},$$

$$3 \text{ TeV CLIC} \quad |g_{H\gamma\gamma}| \geq 0.0018 \text{ TeV}^{-1}.$$

- What If Not Even a Light Resonance Is Found?

Definitely **new physics**. Unitarity \implies new particle(s) [probably wide resonance(s)] below **1.2 TeV**.

EW chiral Lagrangian [Appelquist, Wu (1995)]

$$\mathcal{L}_{eff}(W, Z, \varphi) = \sum_{i=0}^{14} \mathcal{L}^{(i)} = \sum_{i=0}^{14} \alpha_i \mathcal{O}(W, Z, \varphi)$$
$$(\varphi^\pm \sim W_L^\pm, \varphi^0 \sim Z_L^0).$$

SM: $\alpha_i = 0$.

- ★ Measuring α_i can obtain information about **nature**.
- ★ A theoretical analysis of the sensitivity of measuring α_i [He, Kuang, Yuan (1996)]:

Collider(s)	$\mathcal{L}^{(2)l}$	$\mathcal{L}_{1,13}$	\mathcal{L}_2	\mathcal{L}_3	$\mathcal{L}_{4,5}$	$\mathcal{L}_{6,7}$	$\mathcal{L}_{8,14}$	\mathcal{L}_9	\mathcal{L}_{10}	$\mathcal{L}_{11,12}$	$T_1 \parallel B$	Processes
LEP-I (S,T,U)	\perp	$\perp \dagger$					$\perp \dagger$				$g^4 \frac{f_\pi^2}{\Lambda^2}$	$e^-e^+ \rightarrow Z \rightarrow f\bar{f}$
LEP-II	\perp	\perp	\perp	\perp			\perp	\perp		\perp	$g^4 \frac{f_\pi^2}{\Lambda^2}$	$e^-e^+ \rightarrow W^-W^+$
LC(0.5)/LHC(14)			\checkmark	\checkmark			Δ	\checkmark		Δ	$g^2 \frac{E^2}{\Lambda^2} \parallel g^2 \frac{M_W^2}{E^2}$ $g^3 \frac{E f_\pi}{\Lambda^2} \parallel g^2 \frac{M_W}{E}$	$f\bar{f} \rightarrow W^-W^+/(LL)$ $f\bar{f} \rightarrow W^-W^+/(LT)$
LC(1.5)/LHC(14)		Δ	Δ	\checkmark	\checkmark	\checkmark	Δ	\checkmark	\checkmark	\checkmark	$g^2 \frac{1}{f_\pi} \frac{E^2}{\Lambda^2} \parallel g^3 \frac{M_W}{E^2}$ $g^3 \frac{E}{\Lambda^2} \parallel g^3 \frac{M_W^2}{E^3}$ $g^2 \frac{1}{f_\pi} \frac{E^2}{\Lambda^2} \parallel g^3 \frac{M_W}{\Lambda^2}$ $g^3 \frac{E}{\Lambda^2} \parallel g^3 \frac{f_\pi M_W}{E}$ $\frac{E^2}{f_\pi^2} \frac{E^2}{\Lambda^2} \parallel g^2$ $g \frac{E}{f_\pi} \frac{E^2}{\Lambda^2} \parallel g^2 \frac{M_W}{E}$ $\frac{E^2}{f_\pi^2} \frac{E^2}{\Lambda^2} \parallel g^2$ $g \frac{E}{f_\pi} \frac{E^2}{\Lambda^2} \parallel g^2 \frac{M_W}{E}$ $\frac{E^2}{f_\pi^2} \frac{E^2}{\Lambda^2} \parallel g^2 \frac{E^2}{\Lambda^2}$ $g \frac{E}{f_\pi} \frac{E^2}{\Lambda^2} \parallel g^2 \frac{M_W E}{\Lambda^2}$	$f\bar{f} \rightarrow W^-W^+Z/(LLL)$ $f\bar{f} \rightarrow W^-W^+Z/(LLT)$ $f\bar{f} \rightarrow ZZZ/(LLL)$ $f\bar{f} \rightarrow ZZZ/(LLT)$ $W^-W^\pm \rightarrow W^-W^\pm/(LLLL) \dagger$ $W^-W^\pm \rightarrow W^-W^\pm/(LLLT) \dagger$ $W^-W^+ \rightarrow ZZ \& \text{perm.}/(LLLL)$ $W^-W^+ \rightarrow ZZ \& \text{perm.}/(LLLT)$ $ZZ \rightarrow ZZ/(LLLL)$ $ZZ \rightarrow ZZ/(LLLT)$
LHC(14)		Δ	Δ	\checkmark	\checkmark		Δ	Δ	\checkmark	\checkmark	$g^2 \frac{E^2}{\Lambda^2} \parallel g^2 \frac{M_W^2}{E^2}$ $g^3 \frac{E f_\pi}{\Lambda^2} \parallel g^2 \frac{M_W}{E}$ $g^2 \frac{1}{f_\pi} \frac{E^2}{\Lambda^2} \parallel g^3 \frac{M_W}{E^2}$ $g^3 \frac{E}{\Lambda^2} \parallel g^3 \frac{M_W^2}{E^3}$ $g^2 \frac{1}{f_\pi} \frac{E^2}{\Lambda^2} \parallel g^3 \frac{M_W}{E^2}$ $g^3 \frac{E}{\Lambda^2} \parallel g^3 \frac{M_W}{E^2}$	$q\bar{q}' \rightarrow W^\pm Z/(LL)$ $q\bar{q}' \rightarrow W^\pm Z/(LT)$ $q\bar{q}' \rightarrow W^-W^+W^\pm/(LLL)$ $q\bar{q}' \rightarrow W^-W^+W^\pm/(LLT)$ $q\bar{q}' \rightarrow W^\pm ZZ/(LLL)$ $q\bar{q}' \rightarrow W^\pm ZZ/(LLT)$
LC($e^- \gamma$)		\checkmark	\checkmark	\checkmark			\checkmark	\checkmark		\checkmark	$e g^2 \frac{E}{\Lambda^2} \parallel e g^2 \frac{M_W^2}{E^2}$	$e^- \gamma \rightarrow \nu_e W^- Z, e^- W W/(LL)$
LC($\gamma \gamma$)		\checkmark	\checkmark	\checkmark			\checkmark	\checkmark			$e^2 \frac{E^2}{\Lambda^2} \parallel e^2 \frac{M_W^2}{E^2}$ $e^2 g \frac{E f_\pi}{\Lambda^2} \parallel e^2 \frac{M_W}{E}$	$\gamma \gamma \rightarrow W^-W^+/(LL)$ $\gamma \gamma \rightarrow W^-W^+/(LT)$

★ Monte Carlo simulations: 1σ sensitivities at LHC and ILC:

[TESLA TDR] 2-parameter fit:

LHC ($\int \mathcal{L} dt = 100 \text{ fb}^{-1}$) :

$$\alpha_4 < -0.0011 \text{ or } \alpha_4 > 0.011, \quad \alpha_5 < -0.0022 \text{ or } \alpha_5 > 0.0076$$

800 GeV TESLA ($\int \mathcal{L} dt = 1000 \text{ fb}^{-1}$) :

$$\alpha_4 < -0.0070 \text{ or } \alpha_4 > 0.0051, \quad \alpha_5 < -0.0025 \text{ or } \alpha_5 > 0.0019$$

[2005 International LC Workshop, Stanford] 5-parameter fit:

ILC ($\int \mathcal{L} dt = 1000 \text{ fb}^{-1}$) :

$$\alpha_4 < -0.017 \text{ or } \alpha_4 > 0.015, \quad \alpha_5 < -0.016 \text{ or } \alpha_5 > 0.015,$$

$$\alpha_6 < -0.025 \text{ or } \alpha_6 > 0.035, \quad \alpha_7 < -0.020 \text{ or } \alpha_7 > 0.021,$$

$$\alpha_{10} < -0.035 \text{ or } \alpha_{10} > 0.029.$$

- The measured **effective couplings** (**sensitivity is crucial**) reflect certain properties of the **nature**. Checking what model can lead to the measured **effective couplings** \implies clue of finding out the **right new physics model**.

V. SUMMARY

- **EWSBM** is not clear. **New physics** \sim **TeV**.
- **LHC** and **LC** may explore **EWSBM** and discover **new physics**.
- Signals of known **new physics** models have been intensively studied. More studies needed.
- If **LHC** and **LC** only find a light Higgs, testing effective Higgs couplings may help to explore **new physics**.
- If **LHC** and **LC** find not even a light Higgs, studying **EW chiral Lagrangian** may help to explore **new physics**.
- After finding **new physics**, particle physics will be in **exciting** new era.

Thanks !